



**IBM**

*Reference Manual*

**FORTRAN      Automatic Coding System**  
**for the IBM 704 Data Processing System**

**IBM Reference Manual**  
**FORTRAN      AUTOMATIC CODING SYSTEM**  
**FOR THE IBM 704 DATA PROCESSING SYSTEM**

**A JOINT DEVELOPMENT OF**

INTERNATIONAL BUSINESS MACHINES CORPORATION

and

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**MINOR REVISION**  
**(October, 1958)**

This edition, Form No. C28-6003, is a minor revision of the preceding edition 32-7026-1 but does not obsolete it or 32-7026. The principal changes to the former edition are:

*page*

- 11 The statement of the restriction on the value of a subscript expression has been revised.
- 22 Under *Transfer of Control and DOs*, the paragraph headed "EXCEPTION" has been revised.
- 33 The section "READ TAPE" has been revised.
- 43 At the beginning of the section "Optimisation of Arithmetic Expressions," several paragraphs have been added on indicating the order of fixed point multiplication and division.
- 47 The following sections have been added: "Concept of Relative Constant Definition," "Restrictions on Relative Constant Definitions in READ TAPE Lists," "Restriction on Relative Constant Definitions in READ DRUM Lists," and "Restrictions on Relative Constant Definitions in READ and READ INPUT TAPE Lists."
- 48 The section "Limits on the Size of the Source Program" has been revised and extended.

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## **THE FORTRAN SYSTEM**

*The IBM Mathematical Formula Translating System FORTRAN is an automatic coding system for the IBM 704 Data Processing System. More precisely, it is a 704 program which accepts a source program written in the FORTRAN language, closely resembling the ordinary language of mathematics, and which produces an object program in 704 machine language, ready to be run on a 704.*

*FORTRAN therefore in effect transforms the 704 into a machine with which communication can be made in a language more concise and more familiar than the 704 language itself. The result should be a considerable reduction in the training required to program, as well as in the time consumed in writing programs and eliminating their errors.*

*Among the features which characterize the FORTRAN system are the following.*

### **Size of Machine Required**

*The system has been designed to operate on a "small" 704, but to write object programs for any 704. (For further details, see the section on Source and Object Machines in Chapter 7.) If an object program is produced which is too large for the machine on which it is to be run, the programmer must subdivide the program.*

### **Efficiency of the Object Program**

*Object programs produced by FORTRAN will be nearly as efficient as those written by good programmers.*

### **Scope of Applicability**

*The FORTRAN language is intended to be capable of expressing any problem of numerical computation. In particular, it deals easily with problems containing*

*large sets of formulae and many variables, and it permits any variable to have up to three independent subscripts.*

*However, for problems in which machine words have a logical rather than a numerical meaning it is less satisfactory, and it may fail entirely to express some such problems. Nevertheless, many logical operations not directly expressible in the FORTRAN language can be obtained by making use of the provisions for incorporating library routines.*

**Inclusion of  
Library  
Routines**

*Pre-written routines to evaluate any single-valued functions of any number of arguments can be made available for incorporation into object programs by placing them on the master FORTRAN tape.*

**Provision for  
Input and Output**

*Certain statements in the FORTRAN language cause the object program to be equipped with its necessary input and output programs. Those which deal with decimal information include conversion to or from binary, and permit considerable freedom of format in the external medium.*

**Nature of  
Fortran  
Arithmetic**

*Arithmetic in the object program will generally be performed with single-precision 704 floating point numbers. These numbers provide 27 binary digits (about 8 decimal digits) of precision, and may have magnitudes between approximately  $10^{-38}$  and  $10^{38}$ , and zero. Fixed point arithmetic, but for integers only, is also provided.*

## CHAPTER 1. GENERAL PROPERTIES OF A FORTRAN SOURCE PROGRAM

A FORTRAN source program consists of a sequence of FORTRAN *statements*. There are 32 different types of statement, which are described in detail in the chapters which follow.

### Example of a Fortran Program

The following brief program will serve to illustrate the general appearance and some of the properties of a FORTRAN program. It is shown as coded on a standard FORTRAN coding sheet.

	FOR COMMENT	CONTINUATION	FORTRAN STATEMENT	IDENTI- FICATION
1	5	6		72 73 80
	C		PROGRAM FOR FINDING THE LARGEST VALUE	
	C	X	ATTAINED BY A SET OF NUMBERS	
			BIGA = A(1)	
			DO 20 I = 2,N	
			IF (BIGA - A(I)) 10, 20, 20	
10			BIGA = A(I)	
20			CONTINUE	

This program examines the set of  $n$  numbers  $a_i$  ( $i=1, \dots, n$ ) and sets the quantity BIGA to the largest value attained in the set. It begins (after a comment describing the program) by setting BIGA equal to  $a_1$ . Next the DO statement causes the succeeding statements to and including statement 20 to be carried out repeatedly, first with  $i=2$ , then with  $i=3$ , etc., and finally with  $i=n$ . During each repetition of this loop the IF statement compares BIGA with  $a_i$ ; if BIGA is less than  $a_i$ , statement 10, which replaces BIGA by  $a_i$ , is executed before continuing.

### Keypunching the Program

Each statement is punched on a separate card. If a statement is too long to fit on a single card it can be continued over as many as 9 additional *continuation* cards. For each statement the initial card must contain either a zero or a blank in column 6; on continuation cards column 6 must not contain a zero or a blank, and it should be used to number the continuation cards consecutively from 1 to 9.

If a statement is too long to fit on a single line of the coding form, the programmer can signal to the keypuncher that he has continued on to the next line by placing a mark in the column labeled CONTINUATION.

The order of the statements is governed solely by the order of the cards. However, any number less than  $2^{15}$  ( $=32768$ ) may be associated with any statement by punching it in columns 1-5 of the initial card bearing that statement. Thereupon this number becomes the *statement number* of that statement. Statement numbers, besides permitting cross-references within the source program, also help the programmer to correlate the object program with his source program.

Punching the character C in column 1 will cause the card to be ignored by FORTRAN. Such cards may therefore be used to carry comments which will appear when the deck is listed.

Columns 73-80 are not read by FORTRAN and may be punched with any desired identifying information.

The statements themselves are punched in columns 7-72, both on initial and continuation cards. Thus a statement consists of not more than  $10 \times 66 = 660$  characters. A table of the admissible characters in FORTRAN is given in Appendix A.

Blank characters, except in column 6, are simply ignored by FORTRAN, and the programmer may use blanks freely to improve the readability of his FORTRAN listing.

The actual input to FORTRAN is either this deck of cards or a BCD tape written from it on the 704 peripheral card-to-tape equipment with the standard SHARE 80 x 84 board. On the tape an End of File mark after the last card is required.

### **Preview of the Fortran Statements**

The 32 types of statement, of which every FORTRAN program is composed, may be classified as follows.

1. The *arithmetic formula*, which causes the object program to carry out a numerical computation. Chapter 2 discusses the symbols available for referring to constants and variables, and Chapter 3 the combining of these into arithmetic formulas.
2. The 15 *control statements*, which govern the flow of control in the object program. These are discussed in Chapter 4.
3. The 13 *input-output statements*, which provide the object program with its necessary input and output routines. These are discussed in Chapter 5.
4. Finally, the 3 *specification statements*, which provide various information required or desirable to make the object program efficient, are discussed in Chapter 6.

Chapters 7 and 8, which conclude the manual, give additional detail on various topics and examples of FORTRAN programming.



## CHAPTER 2. THE FORTRAN LANGUAGE: Constants, Variables, and Subscripts

Any programming language must provide for expressing numerical constants and variable quantities. FORTRAN also provides a subscript notation for expressing 1, 2, or 3-dimensional arrays of variables.

### Constants

Two types of constant are permissible: fixed point (restricted to integers) and floating point (characterized by being written with a decimal point).

#### *Fixed Point Constants.*

GENERAL FORM	EXAMPLES
1 to 5 decimal digits. A preceding + or — sign is optional. The magnitude of the constant must be less than 32768.	3 +1 –28987

Any unsigned fixed point constant may be used as a statement number.

#### *Floating Point Constants.*

GENERAL FORM	EXAMPLES
Any number of decimal digits, with a decimal point at the beginning, at the end, or between two digits. A preceding + or — sign is optional. A decimal exponent preceded by an E may follow.	17. 5.0 –.0003 5.0E3 (= 5.0 x 10 <sup>3</sup> ) 5.0E+3 (= 5.0 x 10 <sup>3</sup> ) 5.0E–7 (= 5.0 x 10 <sup>–7</sup> )

The magnitude of the number thus expressed must be zero, or must lie between the approximate limits of 10<sup>–38</sup> to 10<sup>38</sup>. The number will appear in the object program as a normalised single-precision floating point number.

**Variables**

Two types of variable are also permissible: fixed point (restricted to integral values) and floating point. Fixed point variables are distinguished by the fact that their first character is I, J, K, L, M, or N.  $I \rightarrow N$

*Fixed Point Variables.*

GENERAL FORM	EXAMPLES
1 to 6 alphabetic or numeric characters (not special characters) of which the first is I, J, K, L, M, or N.	I M2 JOBNO

A fixed point variable can assume any integral value whose magnitude is less than 32768. However, see the section on Fixed Point Arithmetic in Chapter 7.

WARNING. The name of a variable must not be the same as the name of any *function* used in the program after the terminal F of the function name has been removed. Also, if a *subscripted* variable has 4 or more characters in its name, the last of these must not be an F. (For the meaning of “function” and “subscripted” see Chapter 3 and the last section of this chapter.)

*Floating Point Variables.*

GENERAL FORM	EXAMPLES
1 to 6 alphabetic or numeric characters (not special characters) of which the first is alphabetic but not I, J, K, L, M, or N.	A B7 DELTA

A floating point variable can assume any value expressible as a normalised 704 floating point number; i.e. zero, or with magnitude between approximately  $10^{-38}$  and  $10^{38}$ .

WARNING. The restrictions on naming fixed point variables also apply to floating point variables.

**Subscripts and Subscripted Variables**

A variable can be made to represent any member of a 1, 2, or 3-dimensional array of quantities by appending to it 1, 2, or 3 *subscripts*; the variable is then a *subscripted variable*. The subscripts are fixed point quantities whose values determine which member of the array is being referred to.

*Subscripts.*

GENERAL FORM	EXAMPLES
Let $v$ represent any fixed point variable and $c$ (or $c'$ ) any unsigned fixed point constant. Then a subscript is an expression of one of the forms: $v$ $c$ $v + c$ or $v - c$ $c * v$ $c * v + c'$ or $c * v - c'$	$1$ $3$ $MU + 2$ $MU - 2$ $5 * J$ $5 * J + 2$ $5 * J - 2$

The symbol  $*$  denotes multiplication. The variable  $v$  must not itself be subscripted.

*Subscripted Variables.*

GENERAL FORM	EXAMPLES
A fixed or floating point variable followed by parentheses enclosing 1, 2, or 3 subscripts separated by commas.	$A(I)$ $K(3)$ $BETA(5 * J - 2, K + 2, L)$

For each variable that appears in subscripted form the size of the array (i.e. the maximum values which its subscripts can attain) must be stated in a DIMENSION statement (see Chapter 6) preceding the first appearance of the variable.

The value of a subscript expression exclusive of the addend must be greater than zero and not greater than the corresponding array dimension.

*Arrangement of Arrays in Storage.*

A 2-dimensional array  $A$  will, in the object program, be stored sequentially in the order  $A_{1,1}, A_{2,1}, \dots, A_{m,1}, A_{1,2}, A_{2,2}, \dots, A_{m,2}, \dots, A_{m,n}$ . Thus it is stored "columnwise", with the first of its subscripts varying most rapidly, and the last varying least rapidly. The same is true of 3-dimensional arrays. 1-dimensional arrays are of course simply stored sequentially. All arrays are stored backwards in storage; i.e. the above sequence is in the order of decreasing absolute location.

**CHAPTER 3. THE FORTRAN LANGUAGE:  
*Functions, Expressions, Arithmetic Formulas  
 and Function Statements***

Of the various FORTRAN statements it is the *arithmetic formula* which defines a numerical calculation which the object program is to do. A FORTRAN arithmetic formula resembles very closely a conventional arithmetic formula; it consists of the variable to be computed, followed by an = sign, followed by an arithmetic *expression*. For example, the arithmetic formula

$$Y = A - \text{SINF}(B - C)$$

means “replace the value of y by the value of a-sin(b-c)”.

**Functions**

As in the above example, a FORTRAN expression may include the name of a *function* (e.g. the sine function SINF), provided that the routine for evaluating the function is either built into FORTRAN, or is accessible to it as a pre-written subroutine in 704 language on the master FORTRAN tape, or has been defined in a *function statement* (see the last section of this chapter).

GENERAL FORM	EXAMPLES
The name of the function is 4 to 7 alphabetic or numeric characters (not special characters), of which the last must be F and the first must be alphabetic. Also, the first must be X if and only if the value of the function is to be fixed point. The name of the function is followed by parentheses enclosing the arguments (which may be expressions), separated by commas.	SINF(A+B) SOMEF(X,Y) SQRTF(SINF(A)) XTANF(3.*X)

*Mode of a Function and its Arguments.* Consider a function of a single argument. It may be desired to state the argument either in fixed or floating point; similarly the function itself may be in either of these modes. Thus a function of a single argument has 4 possible mode configurations; in general a function of n arguments will have  $2^{n+1}$  mode configurations.

A separate name must be given, and a separate routine must be available, for each of the mode configurations which is used. Thus a complete set of names for the sine function might be

SINOF	Fixed argument, floating function
SIN1F	Floating " , " "
XSINOF	Fixed " , fixed "
XSIN1F	Floating " , " "

The X's and F's are compulsory, but the rest of the naming is arbitrary.

*Built-in Functions.* The FORTRAN system has the routines for evaluating certain functions built in. The following 18 built-in subroutines are always compiled into the object program as open subroutines.

TYPE OF FUNCTION	DEFINITION	NO. OF ARGS	NAME	MODE OF FUNCTION	
				ARGUMENT	FUNCTION
Absolute value	Arg	1	ABSF	Floating	Floating
			XABSF	Fixed	Fixed
Truncation	Sign of Arg times largest integer $\leq  Arg $	1	INTF	Floating	Floating
			XINTF	Floating	Fixed
Remaindering (see note below)	$Arg_1 \text{ (mod } Arg_2)$	2	MODF	Floating	Floating
			XMODF	Fixed	Fixed
Choosing largest value	$\text{Max } (Arg_1, Arg_2, \dots)$	$\geq 2$	MAXOF	Fixed	Floating
			MAX1F	Floating	Floating
			XMAXOF	Fixed	Fixed
			XMAX1F	Floating	Fixed
Choosing smallest value	$\text{Min } (Arg_1, Arg_2, \dots)$	$\geq 2$	MINOF	Fixed	Floating
			MIN1F	Floating	Floating
			XMINOF	Fixed	Fixed
			XMIN1F	Floating	Fixed
Float	Float fixed number	1	FLOATF	Fixed	Floating
Fix	Same as XINTF	1	XFIXF	Floating	Fixed
Transfer of sign	Sign of $Arg_2$ times $Arg_1$	2	SIGNF	Floating	Floating
		2	XSIGNF	Fixed	Fixed

NOTE. The function MODF ( $Arg_1, Arg_2$ ) is defined as  $Arg_1 - [Arg_1/Arg_2] Arg_2$ , where  $[x] =$  integral part of  $x$ .

*Functions on the Library Tape.* Besides the built-in routines, any single-valued function of any number of arguments can be made available to the programmer by placing the appropriate routine on the master FORTRAN tape.

Any such routine will be compiled into the object program as a closed subroutine. In the section on Writing Subroutines for the Master Tape in Chapter 7 are given the specifications which any such routine must meet.

## Expressions

An expression is any sequence of constants, variables (subscripted or not subscripted), and functions, separated by operation symbols, commas, and parentheses so as to form a meaningful mathematical expression.

However, one special restriction does exist. A FORTRAN expression may be either a fixed or a floating point expression, but it must not be a mixed expression. This does not mean that a floating point quantity can not appear in a fixed point expression, or vice versa, but rather that a quantity of one mode can appear in an expression of the other mode only in certain ways. Briefly, a floating point quantity can appear in a fixed point expression only as an argument of a function; a fixed point quantity can appear in a floating point expression only as an argument of a function, or as a subscript, or as an exponent.

*Formal Rules for Forming Expressions.* By repeated use of the following rules, all permissible expressions may be derived.

1. Any fixed point (floating point) constant, variable, or subscripted variable is an expression of the same mode. Thus 3 and I are fixed point expressions, and ALPHA and A(I,J,K) are floating point expressions.
2. If SOMEF is some function of n variables, and if E, F, . . . , H are a set of n expressions of the correct modes for SOMEF, then SOMEF (E, F, . . . , H) is an expression of the same mode as SOMEF.
3. If E is an expression, and if its first character is not + or -, then +E and -E are expressions of the same mode as E. Thus -A is an expression, but +-A is not.
4. If E is an expression, then (E) is an expression of the same mode as E. Thus (A), ((A)), (((A))), etc. are expressions.
5. If E and F are expressions of the same mode, and if the first character of F is not + or -, then

$$\begin{aligned} E + F \\ E - F \\ E * F \\ E / F \end{aligned}$$

are expressions of the same mode. Thus A-+B and A/+B are not expressions. The characters +, -, \*, and / denote addition, subtraction, multiplication, and division.

6. If E and F are expressions, and F is not floating point unless E is too, and the first character of F is not + or -, and neither E nor F is of the form  $A**B$ , then

$$E**F$$

is an expression of the same mode as E. Thus  $A**(B**C)$  is an expression, but  $I**(B**C)$  and  $A**B**C$  are not. The symbol  $**$  denotes exponentiation; i.e.  $A**B$  means  $A^B$ .

*Hierarchy of Operations.* When the hierarchy of operations in an expression is not completely specified by parentheses, then it is understood to be in the following order (from innermost operations to outermost):

Exponentiation

Multiplication and Division

Addition and Subtraction

For example, the expression

$$A + B/C + D**E * F - G$$

will be taken to mean

$$A + (B/C) + (D^E * F) - G.$$

*Ordering within a Hierarchy.* Parentheses which have been omitted from a sequence of consecutive multiplications and divisions (or consecutive additions and subtractions) will be understood to be grouped from the left. Thus, if . represents either \* or / (or either + or -), then

$$A.B.C.D.E$$

will be taken to mean

$$(((A.B).C).D).E)$$

*Verification of Correct Use of Parentheses.* The following procedure is suggested for checking that the parentheses in a complicated expression correctly express the desired operations.

Label the first open parenthesis "1"; thereafter, working from left to right, increase the label by 1 for each open parenthesis and decrease it by 1 for each closed parenthesis. The label of the last parenthesis should be 0; the mate of an open parenthesis labeled n will be the next parenthesis labeled n-1.

*Optimisation of Arithmetic Expressions.* The efficiency of the object program into which an arithmetic expression is translated may depend upon how the arithmetic expression is written. The section on Optimisation of Arithmetic Expressions in Chapter 7 mentions some of the considerations which affect object program efficiency.

**Arithmetic Formulas**

GENERAL FORM	EXAMPLES
"a=b" where a is a variable (subscripted or not subscripted) and b is an expression.	A(I) = B(I) + SIN(C(I))

The = sign in an arithmetic formula has the meaning "is to be replaced by". An arithmetic formula is therefore a command to compute the value of the right-hand side and to store that value in the storage location designated by the left-hand side.

The result will be stored in fixed or floating point according as the variable on the left-hand side is a fixed or floating point variable.

If the variable on the left is fixed point and the expression on the right is floating point, the result will first be computed in floating point and then truncated and converted to a fixed point integer. Thus, if the result is  $\pm 3.569$  the fixed point number stored will be  $\pm 3$ , not  $\pm 4$ . If the variable on the left is floating point and the expression on the right is fixed point, the result will be computed in fixed point, truncated to an integer, and converted to floating point.

*Examples of Arithmetic Formulas.*

FORMULA	MEANING
A=B	Store the value of B in A.
I=B	Truncate B to an integer, convert to fixed point, and store in I.
A=I	Convert I to floating point and store in A.
I=I+1	Add 1 to I and store in I. This example illustrates the point that an arithmetic formula is not an equation but a command to replace a value.
A=MAX1F(SINF(B), COSF(B))	Replace A by the larger of the quantities sinB and cosB. This example illustrates the use of a function as an argument of a function.
A=3.0*B	Replace A by 3B.
A=3*B	Not permitted. The expression is mixed.
A=I*B	Not permitted. The expression is mixed.



## Function Statements

A function may also be defined in the source program itself by means of a function statement, and the definition will then persist throughout that one program. Thus it is possible to have the convenience of the function notation even for functions which are not important enough to deserve a place on the master FORTRAN tape.

GENERAL FORM	EXAMPLES
<p>"a = b" where a is a function name followed by parentheses enclosing its arguments (which must be distinct non-subscripted variables) separated by commas, and b is an expression (see page 14) which does not involve subscripted variables. Any functions appearing in b must be built-in, or available on the master tape, or already defined by preceding function statements.</p>	<pre> FIRSTF(X) = A*X + B SECONDF(X,B) = A*X + B THIRDF(D) = FIRSTF(E)/D FOURTHF(F,G) = SECONDF(F,                 THIRDF(G)) FIFTHF(I,A) = 3.0*A**I SIXTHF(U) = J + K XSIXTHF(U) = J + K </pre>

Just as with ordinary functions, the answer will be expressed in fixed or floating point according as the name does or does not begin with X.

The right-hand side of a function statement may be any expression not involving subscripted variables that meets the requirements specified for expressions. In particular, it may involve functions freely, provided that any such function, if it is not built-in or available on the master tape, has been defined in a *preceding* function statement.

As many as desired of the variables appearing in the expression on the right-hand side may be stated on the left-hand side to be the arguments of the function. Since the arguments are really only dummy variables, their names are unimportant (except as indicating fixed or floating point mode) and may even be the same as names appearing elsewhere in the program.

Those variables on the right-hand side which are not stated as arguments are treated as parameters. Thus, if FIRSTF is defined in a function statement as  $FIRSTF(X) = A*X + B$  then a later reference to FIRSTF(Y) will cause  $ay + b$ , based on the current values of a, b, and y, to be computed. The naming of parameters, therefore, must follow the normal rules of uniqueness.

A function defined by a function statement may be *used* just as any other function. In particular, its arguments may be expressions and may involve subscripted variables; thus a reference to FIRSTF(Z + Y(I)) will cause  $a(z + y_i) + b$ , based on the current values of a, b,  $y_i$ , and z, to be computed.

Functions defined by function statements are always compiled as closed subroutines.

NOTE. All the function statements in a program must precede the first executable statement of the program.

## CHAPTER 4. THE FORTRAN LANGUAGE: Control Statements

The second class of FORTRAN statements is the set of 15 control statements, which enable the programmer to state the flow of his program.

### Unconditional GO TO

GENERAL FORM	EXAMPLES
"GO TO n" where n is a statement number.	GO TO 3

This statement causes transfer of control to the statement with statement number n.

### Assigned GO TO

GENERAL FORM	EXAMPLES
"GO TO n, (n <sub>1</sub> , n <sub>2</sub> , . . . . ., n <sub>m</sub> )" where n is a non-subscripted fixed point variable appearing in a previously executed ASSIGN statement, and n <sub>1</sub> , n <sub>2</sub> , . . . . ., n <sub>m</sub> are statement numbers.	GO TO N, (7, 12, 19)

This statement causes transfer of control to the statement with statement number equal to the value of n last assigned by an ASSIGN statement. The n<sub>1</sub>, n<sub>2</sub>, . . . . ., n<sub>m</sub> are a list of the values which n may be assigned.

The assigned GO TO is used to obtain a pre-set many-way fork.

NOTE: When an assigned GO TO exists in the range of a DO, there is a restriction on the n<sub>1</sub>, n<sub>2</sub>, . . . . ., n<sub>m</sub>. (See the section on DOs in this chapter.)

### ASSIGN

GENERAL FORM	EXAMPLES
"ASSIGN i TO n" where i is a statement number and n is a non-subscripted fixed point variable.	ASSIGN 12 TO N

This statement causes a subsequent GO TO n, (n<sub>1</sub>, . . . , i, . . . , n<sub>m</sub>) to transfer control to the statement whose statement number is i.

The statement ASSIGN 12 TO N and the arithmetic formula  $N = 12$  are *not* the same. A variable which has been assigned can be used only for an assigned GO TO until it is re-established as an ordinary variable.

**Computed  
GO TO**

GENERAL FORM	EXAMPLES
"GO TO ( $n_1, n_2, \dots, n_m$ ), $i$ " where $n_1, n_2, \dots, n_m$ are statement numbers and $i$ is a non-subscripted fixed point variable.	GO TO (30, 40, 50, 60), I

If at the time of execution the value of the variable  $i$  is  $j$ , then control is transferred to the statement with statement number  $n_j$ . Thus, in the example, if  $I$  has the value 3 at the time of execution, a transfer to statement 50 will occur. This statement is used to obtain a computed many-way fork.

**IF**

GENERAL FORM	EXAMPLES
"IF ( $a$ ) $n_1, n_2, n_3$ " where $a$ is any expression and $n_1, n_2, n_3$ are statement numbers.	IF (A/J,K) -B) 10, 20, 30

Control is transferred to the statement with statement number  $n_1, n_2$ , or  $n_3$  according as the value of  $a$  is less than, equal to, or greater than zero.

**SENSE LIGHT**

GENERAL FORM	EXAMPLES
"SENSE LIGHT $i$ " where $i$ is 0, 1, 2, 3, or 4.	SENSE LIGHT 3

If  $i$  is 0, all Sense Lights on the 704 console will be turned OFF; otherwise Sense Light  $i$  will be turned ON.

**IF (SENSE LIGHT)**

GENERAL FORM	EXAMPLES
"IF (SENSE LIGHT $i$ ) $n_1, n_2$ " where $n_1$ and $n_2$ are statement numbers and $i$ is 1, 2, 3, or 4.	IF (SENSE LIGHT 3) 30, 40

Control is transferred to the statement with statement number  $n_1$  or  $n_2$  according as Sense Light  $i$  is ON or OFF, and the Sense Light is turned OFF.

**IF  
(SENSE SWITCH)**

GENERAL FORM	EXAMPLES
"IF (SENSE SWITCH $i$ ) $n_1, n_2$ " where $n_1$ and $n_2$ are statement numbers and $i$ is 1, 2, 3, 4, 5, or 6.	IF (SENSE SWITCH 3) 30, 40

Control is transferred to the statement with statement number  $n_1$  or  $n_2$  according as Sense Switch  $i$  on the 704 console is DOWN or UP.

**IF ACCUMULATOR OVERFLOW**

GENERAL FORM	EXAMPLES
"IF ACCUMULATOR OVERFLOW $n_1, n_2$ " where $n_1$ and $n_2$ are statement numbers.	IF ACCUMULATOR OVERFLOW 30, 40

Control is transferred to the statement with statement number  $n_1$  or  $n_2$  according as the Accumulator Overflow trigger of the 704 is ON or OFF, and the trigger is turned OFF.

**IF QUOTIENT OVERFLOW**

GENERAL FORM	EXAMPLES
"IF QUOTIENT OVERFLOW $n_1, n_2$ " where $n_1$ and $n_2$ are statement numbers.	IF QUOTIENT OVERFLOW 30, 40

Control is transferred to the statement with statement number  $n_1$  or  $n_2$  according as the Multiplier-Quotient Overflow trigger of the 704 is ON or OFF, and the trigger is turned OFF.

**IF DIVIDE CHECK**

GENERAL FORM	EXAMPLES
"IF DIVIDE CHECK $n_1, n_2$ " where $n_1$ and $n_2$ are statement numbers.	IF DIVIDE CHECK 30, 40

Control is transferred to the statement with statement number  $n_1$  or  $n_2$  according as the Divide Check trigger of the 704 is ON or OFF, and the trigger is turned OFF.

**PAUSE**

GENERAL FORM	EXAMPLES
"PAUSE" or "PAUSE $n$ " where $n$ is an unsigned octal fixed point constant.	PAUSE PAUSE 7777

The machine will HALT, with the octal number  $n$  displayed on the 704 console in the address field of the storage register. (If  $n$  is not stated it is taken to be 0.) Pressing the START button causes the program to resume at the next FORTRAN statement.

**STOP**

GENERAL FORM	EXAMPLES
"STOP" or "STOP n" where n is an unsigned octal fixed point constant.	STOP STOP 7777

This statement causes the machine to HALT in such a way that pressing the START button has no effect. Therefore, in contrast to the PAUSE, it is used where a get-off-the-machine stop, rather than a temporary stop, is desired. The octal number n is displayed on the 704 console in the address field of the storage register. (If n is not stated it is taken to be 0.)

**DO**

GENERAL FORM	EXAMPLES
"DO n i = m <sub>1</sub> , m <sub>2</sub> " or "DO n i = m <sub>1</sub> , m <sub>2</sub> , m <sub>3</sub> " where n is a statement number, i is a non-subscripted fixed point variable, and m <sub>1</sub> , m <sub>2</sub> , m <sub>3</sub> are each either an unsigned fixed point constant or a non-subscripted fixed point variable. If m <sub>3</sub> is not stated it is taken to be 1.	DO 30 I = 1, 10 DO 30 I = 1, M, 3

The DO statement is a command to "DO the statements which follow, to and including the statement with statement number n, repeatedly, the first time with  $i = m_1$  and with i increased by  $m_3$  for each succeeding time; after they have been done with i equal to the highest of this sequence of values which does not exceed  $m_2$  let control reach the statement following the statement with statement number n".

The *range* of a DO is the set of statements which will be executed repeatedly; it is the sequence of consecutive statements immediately following the DO, to and including the statement numbered n.

The *index* of a DO is the fixed point variable i, which is controlled by the DO in such a way that its value begins at  $m_1$  and is increased each time by  $m_3$  until it is about to exceed  $m_2$ . Throughout the range it is available for computation, either as an ordinary fixed point variable or as the variable of a subscript. During the last execution of the range, the DO is said to be *satisfied*.

Suppose, for example, that control has reached statement 10 of the program

```

10   DO 11 I = 1, 10
11   A(I) = I*N(I)
12
```

The range of the DO is statement 11, and the index is I. The DO sets I to 1 and control passes into the range.  $N(1)$  is computed, converted to floating point, and stored in  $A(1)$ . Now, since statement 11 is the last statement in the range of the DO and the DO is unsatisfied, I is increased to 2 and control returns to the beginning of the range, statement 11.  $2N(2)$  is computed and stored in  $A(2)$ . This continues until statement 11 has been executed with  $I = 10$ . Since the DO is satisfied, control now passes to statement 12.

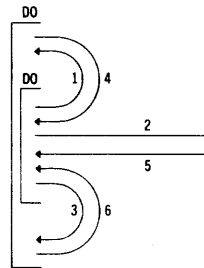
*DOs within DOs.* Among the statements in the range of a DO may be other DO statements. When this is so, the following rule must be observed.

**Rule 1.** If the range of a DO includes another DO, then all of the statements in the range of the latter must also be in the range of the former.

A set of DOs satisfying this rule is called a *nest* of DOs.

*Transfer of Control and DOs.* Transfers of control by IF-type or GO TO-type statements are subject to the following rule.

**Rule 2.** No transfer is permitted into the range of any DO from outside its range. Thus, in the configuration below, 1, 2, and 3 are permitted transfers, but 4, 5, and 6 are not.



**EXCEPTION.** There is one situation in which control can be transferred into the range of a DO from outside its range. Suppose control is in the range of the innermost DO of a nest of DOs which are completely nested: i.e., for every pair of DOs in the nest, one contains the other. Suppose also that control is transferred to a section of program, completely outside the nest to which those DOs belong, which makes no change in any of the indexes or indexing parameters (m's) in the nest. Then after the execution of this section of program, control can be transferred back to the range of the same innermost DO from which it originally came. This provision makes it possible to exit temporarily from the range of some DOs to execute a subroutine. An example is given in Chapter 8.

*Restriction on Assigned GO TO's in the Range of a DO.* When an assigned GO TO is in the range of a DO, the statements in the nest to which it may transfer must all be in the *exclusive range* of a single DO, i.e., among those statements in the range of a DO which are not in the range of any DO in its range.

*Preservation of Index Values.* When control leaves the range of a DO in the ordinary way (i.e. by the DO becoming satisfied and control passing on to the next statement after the range) the exit is said to be a *normal* exit. After a normal exit from a DO occurs, the value of the index controlled by that DO is not defined, and the index can not be used again until it is redefined. (See, however, the section on Further Details about DO Statements in Chapter 7.)

However, if exit occurs by a transfer out of the range, the current value of the index remains available for any subsequent use. If exit occurs by a transfer which is in the ranges of several DOs, the current values of all the indexes controlled by those DOs are preserved for any subsequent use.

*Restriction on Calculations in the Range of a DO.* Almost every type of calculation is permitted in the range of a DO. Only one type of statement is not permitted, namely any statement which redefines the value of the index or of any of the indexing parameters (m's). In other words, the indexing of a DO loop must be completely set before the range is entered.

The first statement in the range of a DO must not be non-executable.

**CONTINUE**

GENERAL FORM	EXAMPLES
"CONTINUE"	CONTINUE

CONTINUE is a dummy statement which gives rise to no instructions in the object program. Its most frequent use is as the last statement in the range of a DO, where it provides a statement number which can be referred to in transfers which are desired to become, in the object program, transfers to the indexing instructions at the end of the loop.

As an example of a program which requires a CONTINUE, consider the table search program

```

10 DO 12 I = 1, 100
11 IF(ARG-VALUE(I)) 12, 20, 12
12 CONTINUE
13

```

This program will examine the 100-entry VALUE table until it finds an entry which equals ARG, whereupon it will exit to statement 20 with the successful value of I available for fixed point use; if no entry in the table equals ARG a normal exit to statement 13 will occur. The program

```
10    DO 11 I = 1, 100
11    IF(ARG-VALUE(I)) 11, 20, 11
12
```

would not work since, as stated in the next section, DO-sequencing does not occur if the last statement in the range of a DO is a transfer.

### Summary of Fortran Sequencing

The precise laws which govern the order in which the statements of a FORTRAN program will be executed, and which have been left unstated till now, may be stated as follows.

1. Control begins at the first executable statement.
2. If control is in a statement S, then control will next go to the statement dictated by the *normal sequencing* properties of S. (The normal sequencing for each type of FORTRAN statement is given in Appendix B.)
3. EXCEPTION. If, however, S is the last statement in the range of one or more DOs which are not yet satisfied, and if S is not a transfer (IF-type or GO TO-type statement), then the normal sequencing of S is ignored and *DO-sequencing* occurs; i.e. control will next go to the first statement of the range of the nearest of the unsatisfied DOs, and the index of that DO will be raised.

NOTE. The statements FORMAT, DIMENSION, EQUIVALENCE, and FREQUENCY, which are discussed in the next two chapters, are non-executable statements, and in any question of sequencing are simply to be ignored.

If the last executable statement in the source program is not a STOP or an IF-type or GO TO-type transfer, then the object program will be compiled as if the pseudo-statement PRESS LOAD CARDS button had followed the last executable statement.

WARNING. Every executable statement in the source program (except the first) must have some path of control leading to it; otherwise errors will occur in the compilation of the object program.



## CHAPTER 5. THE FORTRAN LANGUAGE: *Input-Output Statements*

There are 13 FORTRAN statements available for specifying the transmission of information, during the running of the object program, between core storage on the one hand and tapes, drums, and attached card reader, card punch, and printer on the other hand. These 13 statements may be grouped as follows.

1. Five statements (READ, PUNCH, PRINT, READ INPUT TAPE, and WRITE OUTPUT TAPE) call for the transmission of a list of quantities between cores and an external storage medium – cards, printed sheet, or tape – in which information is expressed in Hollerith punch, decimal print, or BCD code, respectively.
2. One statement (FORMAT) is a non-executed statement which defines the information format in the external medium for the above 5 statements.
3. Four more statements (READ TAPE, READ DRUM, WRITE TAPE, and WRITE DRUM) call for ordinary binary transmission of a list of quantities.
4. Finally, there are 3 statements (END FILE, REWIND, and BACKSPACE) for manipulating tapes.

This chapter will first discuss the formation of a list of quantities for transmission, since such a list must appear in each of the 9 statements in groups 1 and 3 above. Next the method of writing a FORMAT statement will be described, and the format which input data to the object program must have. Finally, the statements in groups 1, 3, and 4 will be discussed.

### **Specifying Lists of Quantities**

Each of the 9 statements which call for the transmission of information includes a list of the quantities to be transmitted. This list is ordered, and its order must be the same as the order in which the words of information exist (for input), or will exist (for output), in the external medium.

The formation and meaning of a list is best described by an example.

A, B(3), (C(I), D(I,K), I = 1,10), ((E(I,J), I = 1,10,1), F(J,3), J = 1,K)

Suppose that this list is used with an output statement. Then the information will be written in the external medium in the order

A, B(3), C(1), D(1,K), C(2), D(2,K), . . . . ., C(10), D(10,K),  
 E(1,1), E(2,1), . . . . ., E(10,1), F(1,3),  
 E(1,2), E(2,2), . . . . ., E(10,2), F(2,3), . . . . ., F(K,3).

Similarly, if this list were used with an input statement, the successive words, as they were read from the external medium, would be placed into the sequence of storage locations just given.

Thus the list reads from left to right and with repetition of variables enclosed within parentheses. Only variables, and not constants, may be listed. The repetition is exactly that of DO-repetition, as if each open parenthesis (except subscripting parentheses) were a DO, with indexing given immediately before the mated closed parenthesis, and with range extending up to that indexing information. The order of the above list is the same as of the "program"

```

1  A
2  B(3)
3  DO 5 I = 1, 10
4  C(I)
5  D(I,K)
6  DO 9 J = 1, K
7  DO 8 I = 1, 10, 1
8  E(I,J)
9  F(J,3)

```

Notice that indexing information, as in DOs, consists of 3 constants or fixed point variables, and that the last of these may be omitted, in which case it is taken to be 1.

For a list of the form K, A(K) or K, (A(I), I = 1,K), where an index or indexing parameter itself appears *earlier* in the list of an input statement, the indexing will be carried out with the newly read-in value.

When it is desired to transmit an *entire* array, and in the inverse of its natural order, i.e., in the order  $A_{m,n}, \dots, A_{m,2}, \dots, A_{2,2}, A_{1,2}, A_{m,1}, \dots, A_{2,1}, A_{1,1}$ , etc. (see the section on Arrangement of Arrays in Storage in Chapter 2), then an abbreviated notation may be used; only the name of the array need be given and the indexing information may be omitted. FORTRAN will look to see if a DIMENSION statement (see Chapter 6) has been made about that name; if it has, indexing information to transmit the entire array in the inverse of its natural order will be supplied automatically, while if it has not, only a single variable will be transmitted. Thus, in the example, the entire A-array will be transmitted, including the case where the array consists of a single quantity.

WARNING. The information given in this section applies in its full generality only to lists which are given with the 5 *decimal* statements of group 1. For the *binary* statements WRITE DRUM and READ DRUM only the abbreviated notation mentioned immediately above is permitted; the restrictions which affect lists for WRITE TAPE and READ TAPE are discussed in the section on Lists for Binary Tape Operations in Chapter 7.

## FORMAT

GENERAL FORM	EXAMPLES
"FORMAT (Specification)" where Specification is as described below.	FORMAT (I2/(E12.4, F10.4))

The 5 decimal input-output statements of group 1 contain, in addition to the list of quantities to be transmitted, the statement number of a FORMAT statement, which describes the information format which exists, or is to be produced, in the external medium. It also specifies the type of conversion between binary and decimal which is to be performed. FORMAT statements are not executed, their function being merely to supply information in the object program. Therefore they may be placed anywhere in the source program.

*The Specification.* For the sake of definiteness the details of writing a FORMAT Specification are given for use with a PRINT statement. However, the description is valid for any case simply by generalizing the concept of "printed line" to that of unit record in the external medium. Thus a unit record may be

1. A printed line with a maximum of 120 characters.
2. A punched card with a maximum of 72 characters.
3. A BCD tape record with a maximum of 120 characters.

Three basic types of decimal-to-binary or binary-to-decimal conversion are available:

	INTERNAL	TO OR FROM	EXTERNAL
E	Floating point variable		Floating point decimal
F	Floating point variable		Fixed point decimal
I	Fixed point variable		Decimal integer

The FORMAT specification describes the line to be printed by giving, for each field in the line (from left to right, beginning with the first type wheel):

1. The type of conversion (E, F, or I) to be used;
2. The width (w) of the field; and
3. For E- and F-conversion, the number of places (d) after the decimal point that are to be rounded and printed. If d is not less than 10 it is treated mod 10.

These basic field specifications are given in the forms

lw, Ew.d, and Fw.d

with the specification for successive fields separated by commas. Thus the statement FORMAT (I2, E12.4, F10.4) might give the line

27 -0.9321E 02 -0.0076

As in this example the field widths may be made greater than necessary, so as to ensure spacing blanks between numbers. In this case there is 1 blank following the 27, 1 blank automatically supplied after the E, and 3 blanks after the 02. Within each field the printed output is always pushed to the extreme right.

It may be desired to print n successive fields in the same fashion. This may be done by giving n before the E, F, or I. Thus the statement FORMAT (I2, 3E12.4) might give

27 -0.9321E 02 -0.7580E-02 0.5536E 00

To permit the repetition of *groups* of field specifications a limited parenthetical expression is permitted. Thus FORMAT (2(F10.6, E10.2), I4) is equivalent to FORMAT (F10.6, E10.2, F10.6, E10.2, I4). No provision is made for parentheses within parentheses.

To permit more general use of F-conversion, a *scale factor* followed by the letter P may precede the specification. The scale factor is so defined that

$$\text{Printed number} = \text{Internal number} \times 10^{\text{Scale factor}}$$

Thus the statement FORMAT (I2, 1P3F11.3), used with the data of the preceding example, would give

27 -932.096 -0.076 5.536

while FORMAT (I2, -1P3F11.3) would give

27 -9.321 -0.001 0.055

A positive scale factor may also be used with E-conversion to increase the number and decrease the exponent. Thus FORMAT (I2, 1P3E12.4) would give with the same data

27 -9.3210E 01 -7.5804E-03 5.5361E-01

NOTE. The scale factor is assumed to be zero if no other value has been given. However, once a value has been given it will hold for all E- and F-conversions following the scale factor within the same FORMAT statement. This applies to both single-record and multi-record formats (see below). Once a scale factor has been given, a subsequent scale factor of zero in the same FORMAT statement must be specified by 0P. Scale factors have no effect on I-conversion.

*Hollerith Fields.* A field may be designated as a Hollerith field, in which case English text will be printed in it. The field width, followed by the desired characters, should appear in the appropriate place in the specification. For example, FORMAT (3HXY = F8.3, 4H Z = F6.2, 7H W/AF = F7.3) would give with the same data

$$XY = -93.210 \quad Z = -0.01 \quad W/AF = 0.554$$

Notice that any Hollerith characters, including blanks, may be printed. This is the sole exception to the statement in Chapter 1 that FORTRAN ignores blanks.

It is possible to print Hollerith information only, by giving no list with the input-output statement and setting up no I, E, or F fields in the FORMAT statement.

Consider a Hollerith field in a FORMAT statement at the time of execution of the object program. If the FORMAT statement is being used with an input statement, the Hollerith text in the FORMAT statement will be replaced with whatever text is read from the corresponding field in the external medium. When the FORMAT statement is used with an output statement, whatever text is currently in the FORMAT statement will be outputted. Thus text can be originated either at source time or at object time by not using, or using, the FORMAT statement with an input statement.

*Multi-Record Formats.* To deal with a *block* of printing a FORMAT specification may have several different line formats, separated by the slash /. Thus FORMAT (3F9.2, 2F10.4/8E14.5) would specify a block in which lines 1, 3, 5, . . . . have format 3F9.2, 2F10.4 and lines 2, 4, 6, . . . . have format 8E14.5.

If a block format is desired having the first two lines of some special formats and all the remaining lines of another format, its last line should be enclosed in parentheses; e.g. FORMAT (I2, 3E12.4/2F10.3, 3F9.4/(10F12.4)).

In general, if there are items in the list still to be transmitted after the format specification has been completely used, the format repeats from the last open parenthesis or (if no parentheses are present) from the beginning.

Blank lines may be introduced into a block by omitting format information; thus // and /// will give 1 and 2 blank lines respectively.

*Ending a FORMAT Statement.* A decimal input-output operation will be brought to an end when and only when a numerical field or the end of the FORMAT statement is encountered and there are no items remaining in the list of the input-output statement itself.

*Carriage Control.* The peripheral printer can operate in 3 modes: single space, double space, and Program Control. Under Program Control, which gives the greatest flexibility, the first character of each BCD record controls the carriage, and that character is not printed. The control characters and their effects are

Blank	Single space before printing
0	Double space before printing
+	No space before printing
1-9	Skip to channels 1-9
J-R	Short skip to channels 1-9

Thus a FORMAT Specification for WRITE OUTPUT TAPE for printing with Program Control will usually begin with 1H followed by the appropriate control character. The same is true of PRINT since in FORTRAN printing on the attached printer simulates Program Control printing on the peripheral printer.

**Data Input  
to the  
Object Program**

Decimal data to be read by a READ or READ INPUT TAPE at the time of execution of the object program must be in essentially the same format as given in the examples of the preceding section. Thus a card to be read with FORMAT (I2, E12.4, F10.4) might be punched

27 -0.9321E 02 -0.0076

Within each field all information must be pushed to the extreme right. Positive signs may be indicated either by a blank or a +; - signs may be punched with an 11-punch or an 8-4 punch (see Appendix A). Blanks in numeric fields are regarded as zeroes. Numbers for E- and F-conversion may contain any number of digits, but only 8 digits of accuracy will be retained. Numbers for I-conversion will be treated mod 32768. To permit economy in punching certain relaxations in input data format are permitted.

1. Numbers for E-conversion need not have 4 columns devoted to the exponent field. The start of the exponent field must be marked by an E, or if that is omitted, by a + or - (not a blank). Thus E2, E02, +2, +02, E 02, and E+02 are all permissible exponent fields.

2. Numbers for E- or F-conversion need not have the decimal point punched. If it is not punched the FORMAT Specification sets its effective position; for example,  $-09321+2$  with E12.4 will be treated as if the decimal point had been punched 4 places before the start of the exponent field, that is between the 0 and the 9. If the decimal point is punched, its position overrides the value of d given in the FORMAT Specification.

## READ

GENERAL FORM	EXAMPLES
"READ n, List" where n is the statement number of a FORMAT statement, and List is as previously described.	READ 30, K, A(K)

The READ statement causes the object program to read cards from the attached card reader. Record after record (card after card) is read until the complete list has been brought in, converted, and stored in the locations specified by the list. The FORMAT statement describes the arrangement of information on the cards and the type of conversion to be done.

If an End of File is encountered (the program attempts to read a card and finds that there is none in the card reader) the object program HALTS. Placing more cards in the card reader and pressing the START button causes the program to continue the reading from the point in the list which it had reached.

A partial check is made in the object program for incorrectly punched columns. Such a column causes a HALT. Pressing the START button causes the faulty column to be treated as a zero, and the program to continue.

## READ INPUT TAPE

GENERAL FORM	EXAMPLES
"READ INPUT TAPE i, n, List" where i is an unsigned fixed point constant between 1 and 10 inclusive or a fixed point variable, n is the statement number of a FORMAT statement, and List is as previously described.	READ INPUT TAPE 3, 30, K, A(K) READ INPUT TAPE I, 30, K, A(K)

The READ INPUT TAPE statement causes the object program to read BCD information from tape unit i, where  $i = 1, 2, \dots, 10$ . Record after record is brought in, in accordance with the FORMAT statement, until the complete list has been placed in storage.

An End of File causes a HALT in the object program. Pressing the START button causes the program to continue the reading from the point in the list which it had reached.

The object program redundancy checks the tape reading. If a record fails twice the program HALTS. Pressing the START button causes the information read on the second attempt to be accepted and the program to continue.

**PUNCH**

GENERAL FORM	EXAMPLES
"PUNCH n, List" where n is the statement number of a FORMAT statement and List is as previously described.	PUNCH 30, (AU), J = 1, 10)

The PUNCH statement causes the object program to punch cards on the attached card punch. Card after card is punched in accordance with the FORMAT statement until the complete list has been punched.

No checking is done, and there are no HALTS in the object program.

**PRINT**

GENERAL FORM	EXAMPLES
"PRINT n, List" where n is the statement number of a FORMAT statement and List is as previously described.	PRINT 30, (AU), J = 1, 10)

The PRINT statement causes the object program to print on the attached printer. Line after line is printed in accordance with the FORMAT statement until the complete list has been printed.

The printing is echo checked. A printing error so detected causes the object program to HALT. Pressing the START button causes the program to continue. Pressing the RESET button and then the START button causes the line to be printed again and the program to continue.

**WRITE  
OUTPUT TAPE**

GENERAL FORM	EXAMPLES
"WRITE OUTPUT TAPE i, n, List" where i is an unsigned fixed point constant between 1 and 10 inclusive or a fixed point variable, n is the statement number of a FORMAT statement, and List is as previously described.	WRITE OUTPUT TAPE 3, 30, (AU), J = 1, 10) WRITE OUTPUT TAPE I, 30, (AU), J = 1, 10)



The WRITE OUTPUT TAPE statement causes the object program to write BCD information on tape unit  $i$ , where  $i = 1, 2, \dots, 10$ . Record after record is written in accordance with the FORMAT statement until the complete list has been written. No End of File is written after the last record.

No checking is done, and there are no HALTS in the object program.

## READ TAPE

GENERAL FORM	EXAMPLES
<p>"READ TAPE <math>i</math>, List" where <math>i</math> is an unsigned fixed point constant between 1 and 10 inclusive or a fixed point variable, and List is as described in Chapter 7.</p>	<p>READ TAPE 3, (AU), J = 1, 10            READ TAPE I, (AU), J = 1, 10</p>

The READ TAPE statement causes the object program to read binary information from tape unit  $i$ , where  $i = 1, 2, \dots, 10$ . Only one record is read, and it will be completely read only if the list contains as many words as the record. The tape, however, always moves all the way to the next record.

The first word of every binary record is copied into an erasable location. This copy serves as an End-of-File test. This means that the binary record must always contain at least one more word than the binary list. If the record has been written by a FORTRAN compiled program, the extra first word is automatically produced. If it is not, care should be taken to write it into the record.

The READ TAPE list should not be longer than the record. If it is, the program may stop with a Read-Write check or it may go on to the next FORTRAN statement. This depends on the size of the list remaining and the extent of indexing instructions required by the list.

If an End-of-File or empty record is encountered while doing FORTRAN reading, the test that occurs with the first word takes care of it. In the End-of-File case, this test causes a halt in the object program. Pressing the START button causes a repetition of this test on the next file. In the Empty Record case, the repetition of the test on the next record occurs automatically. (An empty record may result from a hand-coded program; for example, where two successive write-select tape instructions occur.)

When, by this process, a real record of information is encountered, it is read in according to the list of the READ TAPE instruction. If the instruction has no list, the record is spaced over and the next FORTRAN instruction is executed.

For reasons of timing there are limitations on the complexity of the list. See the section on Lists for Binary Tape Operations in Chapter 7.

The object program redundancy checks the tape reading. (The longitudinal check is applied only if the whole record is read.) If a record fails twice the program HALTS. Pressing the START button causes the information read on the second attempt to be accepted and the program to continue.

## READ DRUM

GENERAL FORM	EXAMPLES
<p>"READ DRUM i, j, List" where i and j are each either an unsigned fixed point constant or a fixed point variable, with the value of i between 1 and 8 inclusive, and List is as described below.</p>	<p>READ DRUM 2, 1000, A, B, C, D READ DRUM I, J, A, B, C, D</p>

The READ DRUM statement causes the object program to read words of binary information from consecutive locations on drum i, where  $i = 1, 2, \dots, 8$ , beginning with the word in drum location j, where  $j = 0, 1, \dots, 2047$ . (If  $j \geq 2048$  it is interpreted mod 2048.) Reading continues until the complete list has been read in.

For reasons of timing there are stringent limitations on the complexity of the list. In fact, the list can employ only the abbreviated notation described earlier in this chapter; it may consist only of variables without subscripts, as A, B, C, D, . . . Those variables which are simple will be read into storage in the ordinary way; those which are arrays will be read with indexing obtained from their DIMENSION statements (see Chapter 6). Thus with READ DRUM the full array must be read in, and in the inverse of natural order.

## WRITE TAPE

GENERAL FORM	EXAMPLES
<p>"WRITE TAPE i, List" where i is an unsigned fixed point constant between 1 and 10 inclusive or a fixed point variable, and List is as described in Chapter 7.</p>	<p>WRITE TAPE 3, (AU), J = 1, 10) WRITE TAPE I, (AU), J = 1, 10)</p>

The WRITE TAPE statement causes the object program to write binary information on tape unit i, where  $i = 1, 2, \dots, 10$ . Only one record is written; its length will be that of the list, except that an extra first word is written to serve in the End-of-File test during reading.

For reasons of timing, there are limitations on the complexity of the list. See the section on Lists for Binary Tape Operations in Chapter 7.

No checking is done, and there are no HALTS in the object program.

### WRITE DRUM

GENERAL FORM	EXAMPLES
<p>“WRITE DRUM <math>i, j, \text{List}</math>” where <math>i</math> and <math>j</math> are each either an unsigned fixed point constant or a fixed point variable, with the value of <math>i</math> between 1 and 8 inclusive, and List is as described for READ DRUM.</p>	<p>WRITE DRUM 2, 1000, A, B, C, D WRITE DRUM I, J, A, B, C, D</p>

The WRITE DRUM statement causes the object program to write words of binary information into consecutive locations on drum  $i$ , where  $i = 1, 2, \dots, 8$ , beginning with drum location  $j$ , where  $j = 0, 1, \dots, 2047$ . (If  $j \geq 2048$  it is interpreted mod 2048.) Writing continues until the complete list has been written.

The list is subject to the same restrictions as for READ DRUM.

No checking is done and there are no HALTS in the object program.

### END FILE

GENERAL FORM	EXAMPLES
<p>“END FILE <math>i</math>” where <math>i</math> is an unsigned fixed point constant between 1 and 10 inclusive or a fixed point variable.</p>	<p>END FILE 3 END FILE I</p>

The END FILE statement causes the object program to write End of File on tape unit  $i$ , where  $i = 1, 2, \dots, 10$ .

### REWIND

GENERAL FORM	EXAMPLES
<p>“REWIND <math>i</math>” where <math>i</math> is an unsigned fixed point constant between 1 and 10 inclusive or a fixed point variable.</p>	<p>REWIND 3 REWIND I</p>

The REWIND statement causes the object program to rewind tape unit  $i$ , where  $i = 1, 2, \dots, 10$ .

**BACKSPACE**

GENERAL FORM	EXAMPLES
"BACKSPACE i" where i is an unsigned fixed point constant between 1 and 10 inclusive or a fixed point variable.	BACKSPACE 3 BACKSPACE I

The BACKSPACE statement causes the object program to backspace tape unit i by one record, where  $i = 1, 2, \dots, 10$ .

**Error Halts**

The several HALTS which can occur during input or output operation in the object program can be identified by the contents of the storage register on the 704 console.

## CHAPTER 6. THE FORTRAN LANGUAGE: *Specification Statements*

The last class of FORTRAN statements is the set of 3 specification statements DIMENSION, EQUIVALENCE, and FREQUENCY. These are statements which are not executed, but which furnish information for use by FORTRAN to make the object program efficient.

### **DIMENSION**

GENERAL FORM	EXAMPLES
"DIMENSION v, v, v, . . ." where each v is a variable subscripted with 1, 2, or 3 unsigned fixed point constants. Any number of v's may be given.	DIMENSION A(10), B(5, 15), C(3, 4, 5)

The DIMENSION statement provides the information necessary to allocate storage in the object program for arrays of quantities.

Every variable which appears in the program in subscripted form must appear in a DIMENSION statement, and the DIMENSION statement must precede the first appearance of the variable. In the DIMENSION statement are given the desired dimensions of the array; in the executed program the subscripts of that variable must never take on values larger than those dimensions.

Thus the example states that B is a 2-dimensional array and that the subscripts of B will never exceed 5 and 15; it causes 75 words of storage to be set aside for the B array.

A single DIMENSION statement may be used to dimension any number of arrays.

## EQUIVALENCE

GENERAL FORM	EXAMPLES
"EQUIVALENCE (a, b, c, ...), (d, e, f, ...), ..." where a, b, c, d, e, f, ... are variables optionally followed by a single unsigned fixed point constant in parentheses.	EQUIVALENCE (A, B(1), C(5)), (D(17), E(3))

The EQUIVALENCE statement enables the programmer, if he wishes, to control the allocation of data storage in the object program. In particular, it permits him to economise on data storage requirements by causing storage locations to be shared by two or more quantities, when the logic of his program permits.

An EQUIVALENCE statement may be placed anywhere in the source program. Each pair of parentheses encloses the names of two or more quantities whose storage locations are to be made the same in the object program; any number of equivalences (pairs of parentheses) may be given.

In an EQUIVALENCE statement the meaning of C(5), for example, is "the 4th storage location in the object program after the cell containing C, or (if C is an array) after C(1) or C(1,1) or C(1,1,1)". In general A(p) is defined for  $p \geq 1$  and means the  $p-1$ th location after A or the beginning of the A array; i.e. the  $p$ th location in the array. If p is not given, it is taken to be 1.

Thus the example statement causes A, B, and C (or the beginnings of the A, B, and C arrays) to be so placed in storage that the location containing A, the location containing B, and the 4th location after that containing C, are the same location. Similarly, it causes the 16th location after D and the 2nd after E both to be another location.

A quantity or array which does not appear in any EQUIVALENCE statement will have storage exclusively to itself.

Locations can be shared only among variables, not among constants.

The sharing of storage locations cannot be planned safely without a knowledge of which FORTRAN statements, when executed in the object program, will cause a new value to be stored in a storage location. There are 7 such statements.

1. Execution of an arithmetic formula stores a new value of the variable on its left-hand side.
2. Execution of an ASSIGN i TO n stores a new value in n.

3. Execution of a DO will in general store a new value of the index. (It will not always do so, however; see the section on Further Details about DO Statements in Chapter 7.)
4. Execution of a READ, READ INPUT TAPE, READ TAPE, or READ DRUM stores new values of the variables listed.

## FREQUENCY

GENERAL FORM	EXAMPLES
"FREQUENCY n(i, j, ...), m(k, l, ...), ..." where n, m, ... are statement numbers and i, j, k, l, ... are unsigned fixed point constants.	FREQUENCY 30(1, 2, 1), 40(11), 50(1, 7, 1, 1)

The FREQUENCY statement permits the programmer to give his estimate, for each branch-point of control, of the frequencies with which the several branches will actually be executed in the object program. This information is used to optimise the use of index registers in the object program.

A FREQUENCY statement may be placed anywhere in the object program, and may be used to give the frequency information about any number of branch-points. For each branch-point the information consists of the statement number of the statement causing the branch, followed by parentheses enclosing the estimated frequencies separated by commas.

Consider the example. This might be a FREQUENCY statement in a program in which statement 30 is an IF, 40 is a DO, and 50 is a computed GO TO. The programmer estimates that the argument of the IF is as likely to be zero as non-zero, and when it is non-zero it is as likely to be negative as positive. The DO statement at 40 is presumably one for which at least one of the indexing parameters (m's) is not a constant but a variable, so that the number of times the loop must be executed to make a normal exit is not known in advance; the programmer here estimates that 11 is a good average for that number. The computed GO TO at 50 is estimated to transfer to its four branches with frequencies 1, 7, 1, 1.

All frequency estimates, except those about DOs, are *relative*; thus they can be multiplied by any constant. The example statement, for instance, could equally well be given as FREQUENCY 30(2,4,2), 40(11), 50(3,21,3,3). A frequency may be estimated as 0; this will be taken to mean that the frequency is very small.

The following table lists the 7 types of statement about which frequency information may be given.

TYPE	NO OF FREQS	REMARKS
Computed GO TO	$\geq 2$	Order of frequencies: same as order of branches
IF	3	" " " " " " " " "
IF (SENSE SWITCH)	2	" " " " " " " " "
IF ACCUMULATOR OVERFLOW	2	" " " " " " " " "
IF QUOTIENT OVERFLOW	2	" " " " " " " " "
IF DIVIDE CHECK	2	" " " " " " " " "
DO	1	To be given only when $m_1$ , $m_2$ , or $m_3$ is variable.

It is not necessary to give frequency information about any branch-point. If none is given, it will be taken that the probabilities of all branches are equal.

A frequency estimate concerning a DO will be ignored except when at least one of the indexing parameters of that DO is variable. Moreover, the frequency estimate should be based only on the expected values of those parameters; in other words, even if the range of the DO contains IFs or GO TOs which may transfer outside the range, the frequency estimate should be the number of times the range must be executed to cause a normal exit.

A DO for which the indexing parameters are variable and for which no FREQUENCY statement is given will be treated as if a frequency of 5 had been estimated.



## CHAPTER 7. MISCELLANEOUS DETAILS ABOUT FORTRAN

### Source and Object Machines

The *source* machine is the 704 on which the source program is translated into the object program. The *object* machine is that on which the object program is run.

The source machine must be at least as large as a "small" 704; i.e. a 704 possessing 4096 words of core storage, floating point instructions, CPA (copy and add logical) instruction, 1 drum unit, 4 tape units, attached card punch, attached or peripheral card reader, and attached or peripheral printer.

The object machine may be of any size. Among the information produced by FORTRAN is a count of the storage locations required by the object program, from which it can be easily decided whether the object program is too large for any given object machine.

### Arrangement of the Object Program

The instructions and constants of the object program begin in lower memory and extend upwards. Data and other storage locations required for the operation of the program begin at location 77777<sub>8</sub> and extend downwards. Thus these latter locations are always at the top of memory, regardless of the size of the object machine.

The topmost section of data storage is occupied by those variables which appear in DIMENSION or EQUIVALENCE statements. The arrangement of this region is such that two programs, whose DIMENSION and EQUIVALENCE statements are identical, will have this region allocated identically. This fact makes it possible to write families of programs which deal with the same data.

The successively lower sections of storage are occupied by variables not mentioned in DIMENSION or EQUIVALENCE statements, then certain storage locations required for the operation of the program, and finally a section of erasable storage.

For each object program FORTRAN produces a printed description of the exact arrangement of storage locations.

### Fixed Point Arithmetic

The use of fixed point arithmetic is governed by the following considerations.

1. Fixed point constants specified in the source program must have magnitudes less than  $2^{15}$ .
2. Fixed point data read in by the object program are treated mod  $2^{15}$ .
3. Fixed point arithmetic in the object program is arithmetic mod  $2^{15}$ .
4. Indexing in the object program is mod (size of the object machine).

## Exponentiation

The appearance of an exponential  $E^{**}F$  in an expression will produce one of 5 object situations.

**1 and 2.** If  $F$  is a fixed point constant from  $+1$  to  $+7$  inclusive, then one of two open subroutines will be compiled, depending upon whether  $E$  is fixed or floating. One or the other of these subroutines will be compiled for each such exponentiation which occurs. These subroutines perform exponentiation by repeated multiplication; they consist of  $F-1$  multiplications and a maximum of  $F+2$  other instructions. The exponential is computed for any  $E$ .

**3 and 4.** If  $F$  is a fixed point constant not in the range  $+1$  to  $+7$  inclusive, or a fixed point variable, then one of two closed subroutines will be compiled, depending upon whether  $E$  is fixed or floating. These subroutines will not appear more than once in the object program. They perform exponentiation by forming  $E^F$  as the appropriate product of  $E, E^2, E^4, E^8, \dots$ , followed (if  $F < 0$ ) by division into 1.

The subroutine for fixed  $E$  has 34 instructions and takes an average of 10 milliseconds. For  $F \leq 0, E = 0$  and for  $F < 0, |E| > 1$ , it returns 0; for all other cases, it returns  $E^F$ .

The subroutine for floating  $E$  has 38 instructions and takes an average of 9 milliseconds. For  $F \leq 0, E = 0$ , it returns 0; for all other cases, it returns  $E^F$ .

**5.** If  $F$ , and therefore  $E$ , is floating, a closed subroutine is compiled. It will not appear more than once in the object program. It produces  $E^F$  as  $e^{F \ln E}$ ; it has 100 instructions and takes approximately 6 milliseconds. For  $F \leq 0, E = 0$ , it returns 0; for all other cases it returns  $|E|^F$ .

## Writing Subroutines for the Master Tape

Library subroutines exist on the master FORTRAN tape in relocatable binary form. Placing a new subroutine on that tape involves (1) producing the routine in the form of relocatable binary cards, and (2) transcribing those cards on to the master tape by means of a program furnished for that purpose.

In the object program transfer to the subroutine is by the sequence

```
TSX  Subroutine, 4
Return
```

The subroutine itself and any constants that it requires should be located in relocatable locations 0, 1, 2,  $\dots$ . It may also make use of a *common storage region* of any desired length  $n$ , beginning with relocatable location  $77777_8-(n-1)$  and ending with relocatable location  $77777_8$ .

At the moment of transfer to the subroutine  $Arg_1$  will have been placed in the

AC, Arg<sub>2</sub> (if it exists) in the MQ, Arg<sub>3</sub> (if it exists) in relocatable location 77775<sub>8</sub> of the common storage region, Arg<sub>4</sub> (if it exists) in relocatable location 77774<sub>8</sub>, etc. The common storage region may also be used for erasable storage by the subroutine.

The output of the subroutine is to be left in the AC, and index registers 1 and 2 must be returned with their original contents.

Fixed point quantities in the object program exist in the following format: sign in sign bit, magnitude in decrement field, remainder of word all zeroes.

It is suggested that error HALTS in subroutines be coded as HPR instructions, permitting the tag and address fields to contain identifying numbers which can be recognised at the console.

### Optimisation of Arithmetic Expressions

Considerable attention is given by the FORTRAN System to the matter of efficiency of the object program arising from an arithmetic expression, regardless of how the expression has been written. Thus, although, as stated earlier (cf. p. 15 under "Ordering within a Hierarchy"), an expression of the form

$$A \cdot B \cdot C \cdot D \cdot E$$

will be taken to mean

$$(((A \cdot B) \cdot C) \cdot D) \cdot E$$

(where  $\cdot$  is  $*$  or  $/$ , or  $+$  or  $-$ ), it is assumed by the system that any *mathematically* equivalent expression is *computationally* equivalent. Hence, a sequence of consecutive multiplications and/or divisions (additions and/or subtractions) not grouped by parentheses will automatically be reordered, if necessary, to minimise the number of storage accesses in the object program.

Although the above stated assumption concerning mathematical vs. computational equivalence is virtually true in regard to floating point expressions, special care must be taken to indicate the order of fixed point multiplication and division, since fixed point arithmetic is "greatest integer" (i.e., remainderless) arithmetic in FORTRAN.

Thus, the expression

$$5 \cdot 4 / 2$$

is taken to mean  $((5 \cdot 4) / 2)$ , but it is computed in a FORTRAN object program as

$$((5 / 2) \cdot 4)$$

i.e., from left to right *after* permutation of the operands to minimise storage accesses. The result of the computation in this case is the integer 8.

On the other hand, the expression

$$(5 \cdot 4) / 2$$

is taken to mean and, in fact, is computed as

$$((5 \cdot 4) / 2)$$

and the result is the integer 10.

Thus, to insure maximum accuracy of fixed point multiplication and division within an otherwise unparenthesised subexpression, judicious insertion of parentheses may be indicated.

Another important type of optimisation, concerned with *common subexpressions*, takes place only if the expression has been suitably written. As an example, consider the arithmetic formula

$$Y = A*B*C + \text{SINF}(A*B)$$

An efficient object program would form the product  $A*B$  only once; yet if the arithmetic formula is written as above, the multiplication of  $A$  by  $B$  will occur twice. The correct way to write this arithmetic formula is

$$Y = (A*B)*C + \text{SINF}(A*B)$$

The common subexpression  $A*B$  has been displayed by the extra pair of parentheses, and an object program will be formed which multiplies  $A$  by  $B$  only once.

In general, when common subexpressions exist in an expression, parentheses should be used to display them.

There is one case where the programmer need not write the parentheses, because FORTRAN will understand that they are there. The parentheses discussed in the section Hierarchy of Operations in Chapter 3 are of this type, and need not be given. Thus

$$Y = A*B + C + \text{SINF}(A*B)$$

is as suitable for optimisation as

$$Y = (A*B) + C + \text{SINF}(A*B)$$

However, the parentheses discussed in the section Ordering within a Hierarchy in Chapter 3 must be supplied if common subexpression optimisation is to occur.

### **Further Details about DO Statements**

This section contains further details about DOs, which may be of interest to the advanced programmer.

*Triangular Indexing.* Indexing such as

```
DO  I = 1,10  
DO  J = 1,10
```

or

```
DO  I = 1,10  
DO  J = 1,I
```

is permitted and simplifies work with triangular arrays. These are simply special cases of the fact that an index under control of a DO is available for general use as a fixed point variable.

The diagonal elements of an array may be picked out by the following type of indexing:

$$\begin{aligned} \text{DO } I = 1, 10 \\ A(I, I) = \text{some expression} \end{aligned}$$

*Status of the Cell Containing I.* A DO loop with index I does not affect the contents of the object program storage location for I except under certain circumstances, namely if

1. An IF-type or GO TO-type transfer exit occurs from the range of the DO;
2. I is used as a variable in the range of the DO; or
3. I is used as a subscript in combination with a *relative constant* whose value changes within the range of the DO. (A relative constant is a subscript the fixed point variable of which is not currently under control of a DO.)

Therefore, if a normal exit occurs from a DO to which cases 2 and 3 do not apply, the I cell contains what it did before the DO was encountered. After normal exit where 2 or 3 do apply, the I cell contains the first value of the I-sequence which exceeds  $m_2$ . After a transfer exit the I cell contains the current value of I.

What has just been said applies only when I is referred to as a *variable*. When it is referred to as a *subscript*, I is undefined after any normal exit and is the current value after any transfer exit.

### **Lists for Binary Tape Operations**

There are restrictions on the complexity of the parenthesised parts of lists for the READ TAPE and WRITE TAPE statements which must be observed if the object program indexing is not to exceed 288 microseconds, the maximum safe time for calculation between CPY instructions on the 704.

Unfortunately this matter is exceedingly complicated and therefore no complete discussion will be given. Instead, certain rules will be given which will permit the construction of lists which can be relied upon to work; there will be other lists, excluded by these rules, which would also work.

Define the term *subscript combination* as follows. Consider each subscript of each subscripted variable to be specified by the four symbols, c, v, c' and d, where d is the maximum value of the subscript as given in the DIMENSION statement about the variable, and where  $c*v \pm c'$  is the full form of the subscript. (The full form of the subscript I would be  $1*I+0$ ; that of the subscript 3 would be  $1*0+3$ , etc.). Then the subscript combination of a subscripted variable is one of the ordered sets

$$\begin{aligned} c_1, v_1 \\ c_1, v_1, c_2, v_2, d_1 \\ c_1, v_1, c_2, v_2, c_3, v_3, d_1, d_2 \end{aligned}$$

depending upon whether the variable has 1, 2, or 3 subscripts. Thus A(I,J,K),

B(I,K,J), C(5\*I,J,K), and D(I,J) all have different subscript combinations, but A(I,J,K) and B(I+5,J,K) have the same subscript combination if the first two dimensions of A and B are the same.

Also, define as an *element* of a list a part bounded by principal commas in the list.

*Elements which Contain no Subscripted Variable.* There are no restrictions on such elements.

*Elements which Contain no Variable with Three Subscripts.* Let

$$\begin{aligned}
 N_1 &= \text{number of different 1-dimensional subscript combinations} \\
 N_2 &= \text{ " " " 2. " " " } \\
 M_1 &= 0 \text{ if } N_1 = 0; \text{ otherwise } M_1 = 1 \\
 M_2 &= 0 \text{ if } N_2 = 0; \text{ otherwise } M_2 = 5
 \end{aligned}$$

Then the restriction is that  $4N_1 + 6N_2 + \max(M_1, M_2)$  must not exceed 18.

For example, the element  $((A(I,J), B(I,J), J = 1,10), C(I), I = 1,10)$  has  $N_1 = 1, N_2 = 1$  (provided that the first dimensions of A and B are the same); hence  $4N_1 + 6N_2 + \max(M_1, M_2) = 15$ , and the element is permissible.

*Elements which Contain Variables with Three Subscripts.* Consider a variable A whose three subscripts  $s_1, s_2, s_3$  involve as variables  $v_1, v_2, v_3$ . Then the skeleton elements

$$((( \quad , v_3 = \quad ), v_2 = \quad ), \quad , v_1 = \quad )$$

or

$$((( \quad , v_3 = \quad ), v_1 = \quad ), \quad , v_2 = \quad )$$

or

$$((( \quad , v_2 = \quad ), v_3 = \quad ), \quad , v_1 = \quad )$$

will work. The innermost parentheses (controlling  $v_3, v_3, v_2$  respectively) may contain  $A(s_1, s_2, s_3)$  and any number of other variables with the same subscript combination; similarly the outermost parentheses may contain variables of any one subscript combination. The middle parentheses may not contain any subscripted variables. Thus for example

$$(((A(I,J,K), B(I,J,K), K = 1,10), J = 1,5), C(I), D(I), I = 1,10)$$

will work provided that the first two dimensions of A and B are the same. This example makes use of the first of the skeleton elements just given.

In the special case where the next element in the list is neither subscripted nor enclosed in controlling parentheses, the first of the above skeleton elements may also contain variables of any one subscript combination in its middle parentheses.

Finally, the skeleton element

$$((( \quad , v_1 = 1, d_1), v_2 = 1, d_2), v_3 = \quad )$$

which unlike the others indexes in the natural order, will work. Notice, however, that the indexing parameters for  $v_1$  and  $v_2$  must be such that the array is swept through consecutively. The innermost parameters may contain  $A(s_1, s_2, s_3)$  and any number of other variables with the same subscript combination.

*Variable Indexing Parameters and Relative Constants.* Another restriction affecting lists for binary tape operations concerns the use of relative constants and of indexing parameters which are variables. (A relative constant is a subscript, the variable of which is not currently under the control of a DO or a controlling parenthesis.)

The restriction is, that variables which have a subscript involving either a relative constant or an index governed by variable indexing parameters may appear only in the *first* element of a list. Furthermore, all such variables must also have among their subscripts one whose index is controlled by the first parenthesis.

For example, in  $((A(I,J), I = 1,L), B(K,J), J = 1,M)$  both the subscripts of A are governed by variable indexing parameters; for B the same is true of one of its subscripts, while the other is a relative constant (unless the READ TAPE or WRITE TAPE is itself in the range of a DO for K). However, since J, which is the index controlled by the first parenthesis, is a subscript of both A and B, this element will work if it is the first element in the list.

**Concept of  
Relative  
Constant  
Definition**

If a fixed-point variable appears in a relative constant anywhere in the program, then any appearance it makes as the left-hand side of an arithmetic formula or in an input list will be called a *relative constant definition*. In the object program some computation will take place at each such definition, and if this definition occurs in a READ TAPE or READ DRUM list, a timing violation may occur unless the following restrictions are observed.

**Restrictions  
on Relative  
Constant  
Definitions  
in READ TAPE  
Lists**

There are two general cases to be distinguished.

- Case 1.** The relative constant occurs in the program only elsewhere than later in the same list with the relative constant definition.
- Case 2.** The relative constant occurs in the same list with the relative constant definition and following it.

*Case 1. Relative Constant Elsewhere than Later in the List.* There are two subcases.

- 1.** Where the relative constant occurs in a 2- or 3-dimensional subscript combination, or in a 1-dimensional subscript expression with a coefficient, the following rule must be observed.

*Rule.* The relative constant definition may be in a READ TAPE list, in any position, except (a) to the left of any DO-implying parenthesis (i.e., a left parenthesis which is not a subscript parenthesis—see page 26), (b) to the left of a non-subscripted array symbol, or (c) within DO-implying parentheses.

2. Where the relative constant occurs in a 1-dimensional subscript expression without a coefficient, the following rule must be observed.

*Rule.* Relative constant definitions in a READ TAPE list are permissible, but there must not be more than five of them where the conditions of the three exceptions above apply.

*Case 2. Relative Constant Later in the List.* The relative constant may follow its definition in the same list only under the following special conditions.

1. The relative constant appears only later in the same list and not elsewhere in the program.
2. The relative constant is 1-dimensional and without a coefficient.
3. An extra pair of parentheses is placed around the relative constant and the symbol which it subscripts.

Examples: The READ TAPE list I, J, K, (B(J, L)) is illegal because the relative constant is 2-dimensional. The list I, A(I), is illegal but becomes legal with extra parentheses; i.e. I, (A (I)).

**Restriction  
on Relative  
Constant  
Definitions  
in READ DRUM  
Lists**

Relative constant definitions may not be to the left of an array symbol in a READ DRUM list.

**Restrictions  
on Relative  
Constant  
Definitions  
in READ and  
READ INPUT  
TAPE Lists**

Where the relative constant definition appears in the same READ or READ INPUT TAPE list with its relative constant and precedes it, extra parentheses may be required in the list. In such a list, it is necessary that there be a left parenthesis, other than the left parenthesis of a subscript combination, between the relative constant definition and its relative constant. If the list does not contain the parenthesis, it may most easily be obtained by placing parentheses around the symbol subscripted by the relative constant.

Examples:

A, B, K, M, (CJ), J = 1, 10), G(K)  
A, B, K, M, G(K)

The first of these two BCD input lists is correct. The second is incorrect, but may be made correct with extra parentheses; i.e.

A, B, K, M, (G(K))

**Limits on the  
Size of the  
Source Program**

In performing the translation from source to object program, FORTRAN forms and uses tables which summarise various aspects of the information contained in the source program. These tables are limited in size, with corresponding limitations on the amount of information which the source program may contain. If a table size is exceeded, the FORTRAN program will HALT at a stop location.



In what follows, the phrase “literal appearance” means that if the same thing appears more than once it must be counted more than once.

1. (TEIFNO Table). The number of FORTRAN statements which have statement numbers must not exceed 1500. (An input or output statement which has a statement number and whose list contains controlling parentheses counts double.)
2. (FIXCON Table). The number of different fixed point constants must not exceed 100. (In this count, constants which differ only in sign are not considered different.)
3. (FLOCON Table). The number of different floating point constants must not exceed 450. (In this count, constants which differ only in sign are not considered different, nor are numbers such as 4., 4.0, 40.E-1, etc., which are really the same number.)
4. (TDO Table). The total number of DOs in a program must not exceed 150. It must be remembered that a DO derives not only from a DO statement but also from DO-implying parentheses in input-output lists.
5. The number of DO statements in any one nest must not exceed 50.
6. (TIFGO Table). The total number of ASSIGNs plus IF-type and GO TO-type statements must not exceed 300.
7. (TRAD Table). The total number of statement numbers mentioned in assigned GO TO and computed GO TO statements must not exceed 250.
8. (FRET Table). The total number of numbers mentioned in FREQUENCY statements must not exceed 750. (Such a statement as FREQUENCY 30(1, 2, 1) has 4 numbers.)
9. (DIM Tables). The total number of 1-, 2-, and 3-dimensional variables which appear in DIMENSION statements must not exceed 100, 100, and 90, respectively.
10. (EQUIT Table). The total number of literal appearances of variables in EQUIVALENCE statements must not exceed 750.
11. (FORMAT Table). Compute the value  $f$  in the following way for each FORMAT statement in the problem. Make a character count of each FORMAT statement, starting at the opening parenthesis and ending at the closing parenthesis. Divide by 6, allowing a remainder to count as 1. Add 1. The total  $f$  values for each problem must not exceed 715.
12. (LAMBDA Table). This table, and the BETA table which follows, limit the size of arithmetic expressions on the right-hand side of arithmetic formulas and as the arguments of IF statements. In any one expression, let
  - $n$  = number of literal appearances of variables and constants, except those in subscripts;
  - $b$  = number of open parentheses, except those introducing subscripts;
  - $p$  = number of appearances of  $+$  or  $-$ , except in subscripts or as unitary operators. (The  $+$  in  $A*(|B)$  is a unitary operator.);
  - $t$  = number of appearances of  $*$  or  $/$ , except in subscripts;
  - $e$  = number of appearances of  $**$ ;
  - $f$  = number of literal appearances of function names;
  - $a$  = number of arguments of functions. (For  $SINF(SINF(X))$ ,  $a = 2$ .)
 Then  $\lambda$ , which equals  $n+4b+4a-3f+3p+2t+e+3$ , must not exceed 400.
13. (BETA Table). With the same definition,  $\beta = \lambda+1-n-f$  must not exceed 300.

- 14.** (ALPHA Table). In order to determine in advance whether an ALPHA table overflow will occur during the course of translation of an arithmetic statement, the following procedure should be carried out. Set the initial value of a counter to 3. Scanning the right-hand side of the statement in question, add 4 to the value of this counter for each left parenthesis encountered and subtract 4 for each right parenthesis encountered. This statement is compilable by the 4K version of the FORTRAN System if and only if the counter value never exceeds 43. This statement is compilable by the 8K version of the FORTRAN System if and only if the counter value never exceeds 139.
- 15.** (CLOSUB Table). In the entire program, the number of literal appearances of functions must not exceed 1500.
- 16.** (FORVAL Table). The total number of literal appearances of non-subscripted fixed point variables on the left-hand side of arithmetic formulas and in input lists must not exceed 500.
- 17.** (FORVAR Table). The total number of literal appearances of non-subscripted fixed point variables on the right-hand side of arithmetic formulas and in the arguments of IFs must not exceed 750.
- 18.** (FORTAG Table). The total number of literal appearances of subscripted variables must not exceed 1500.
- 19.** (TAU Tables). The total number of different 1-, 2-, and 3-dimensional subscript combinations must not exceed 100, 90, and 75, respectively. (See the section "Lists for Binary Tape Operations" for the definition of subscript combination.)
- 20.** (SIGMA Tables). Consider a variable with 3 subscripts, and let the additive parts of these subscripts (when written in full form) be  $c_1'$ ,  $c_2'$ ,  $c_3'$ . Then the number of distinct ordered triples  $(c_1', c_2', c_3')$ , such that at least one  $c_i'$  does not equal zero, must not exceed 99. Similarly, for 2- and 1-dimensional variables, neither the number of distinct ordered couples  $(c_1', c_2')$  nor of distinct  $c_i'$  may exceed 99.
- 21.** (FORSUB Table). The total number of distinct FORTRAN functions (functions defined within the problem by an arithmetic statement) must not exceed 50.
- 22.** (NLIST Table). The total number of unique fixed point variables in assigned GO TO statements must not exceed 25.

The following are tables applying exclusively to FORTRAN II:

- 23.** (SUBDEF Table). This table arises from arguments given in SUBROUTINE and FUNCTION statements. One word is used for each SUBROUTINE or FUNCTION name and one word for each literal appearance of an argument. The number of words must not exceed 900.
- 24.** (COMMON Table). The number of literal appearances of variables in COMMON statements must not exceed 600.
- 25.** (HOLARG Table). This table arises from Hollerith arguments in CALL statements. For every nH in a CALL statement, divide n by 6, adding 1 for any remainder. Add 1 to this. This total for any one program must not exceed 900.
- 26.** (NONEXC Table). The total number of non-executable statements must not be greater than 1500.
- 27.** (TSTOPS Table). The total number of STOP statements must not be greater than 300.

## CHAPTER 8. EXAMPLES OF FORTRAN PROGRAMMING

### A Complete but Simple Program

The example below is the same as that given in Chapter 1, but expanded into a complete program. The purpose of the program is to discover the largest value attained by a set of numbers  $A(I)$  and to print that number on the attached printer. The numbers  $A(I)$  exist on punched cards, 12 to a card, each number occupying a field of 6 columns. There are not more than 999 numbers; the actual number  $N$  is punched on a lead card.

FOR COMMENT STATEMENT NUMBER	CONTINUATION	FORTRAN STATEMENT	IDENTIFICATION	
			72	80
C		PROGRAM FOR FINDING THE LARGEST VALUE		
C	X	ATTAINED BY A SET OF NUMBERS		
		DIMENSION A(999)		
		FREQUENCY 30(2,1,10), 5(100)		
		READ 1, N, (A(I), I = 1,N)		
1		FORMAT (I3/(12F6.2))		
		BIGA = A(1)		
5		DO 20 I = 2,N		
30		IF (BIGA-A(I)) 10,20,20		
10		BIGA = A(I)		
20		CONTINUE		
		PRINT 2, N, BIGA		
2		FORMAT (22H1THE LARGEST OF THESE I3, 12H NUMBERS IS F7.2)		
		STOP 77777		

The first executable statement is the READ; therefore the program begins there. The READ causes first  $N$  and then  $A(1)$ ,  $A(2)$ , . . . . .,  $A(N)$  to be brought in from the card reader, in accordance with the FORMAT statement 1. Notice that the indexing of the loop bringing in  $A$  will work ~~correctly~~, since the indexing parameter  $N$  occurs *earlier* in the list.

The FORMAT statement says that there is first a single card with format I3, followed by any number of cards with format 12F6.2. On the single card  $N$  is punched as a decimal integer in columns 1-3 and is also to be converted into a fixed point number. In the remainder of the deck the numbers  $A(I)$  are punched 12 to a card in columns 1-6, 7-12, etc. Each number is presumably

punched as xxxxx or -xxxxx with the decimal point understood to precede the last two digits. If, however, a column is used for a decimal point, its position overrides this understanding.

After the READ is executed control moves to the next executable statement, the arithmetic formula  $BIGA = A(1)$ . The cell BIGA now contains  $A(1)$ .

Next the DO statement sets  $I$  to 2 and creates a loop starting with the IF and ending with the CONTINUE. The first time the IF is executed it transfers control either to statement 10 or statement 20, according as  $A(2) > BIGA$  or  $A(2) \leq BIGA$ . In the first case, therefore, BIGA becomes  $A(2)$ ; otherwise it remains  $A(1)$ .

Control is now in the CONTINUE, which is the last statement in the range of a DO which is still unsatisfied (provided that  $N > 2$ ), and which is not a transfer. Therefore DO-sequencing occurs:  $I$  is increased to 3 and control goes back to the IF. The comparison now is between BIGA and  $A(3)$ ; if  $A(3)$  is the larger it becomes the new BIGA.

This process continues until control is in the CONTINUE with  $I = N$ . The DO is satisfied; therefore normal sequencing occurs and control moves to the PRINT. BIGA now contains the largest value in the set of  $A$ 's;  $N$  and the  $A$ -array have not been altered.

The PRINT statement causes  $N$  and BIGA to be printed on the attached printer in accordance with the FORMAT statement 2. This statement causes a line to be printed as follows. The carriage control character is a Hollerith "1" which causes a skip to channel 1, bringing the paper to the top of a new sheet. Type wheels 1-21 receive the text 'THE LARGEST OF THESE '; wheels 22-24 receive  $N$  converted back to decimal integer form; wheels 25-36 receive ' NUMBERS IS '; and wheels 37-43 receive BIGA converted into fixed decimal form, with a decimal point preceding the last two digits. Notice that an extra column is allotted to BIGA to allow for the decimal point, which was presumably omitted in the data input.

The program ends with a HALT and  $77777_8$  in the address field of the storage register on the console. Pressing the START button will have no effect.

The only subscripted variable used in the program is  $A$ . Hence DIMENSION  $A(999)$  is the only dimension information required.

The only statements about which a FREQUENCY statement can be made are the IF and the DO. The programmer anticipates that BIGA will usually be greater than  $A(I)$ , a plausible guess if the  $A(I)$  are randomly arranged but not if they tend to increase with increasing  $I$ . He also predicts for the DO that 100 is a reasonable average for  $N$ .

**A DO Nest  
with Exit  
and Return**

Given an  $N \times N$  square matrix  $A$ , to find those off-diagonal elements which are symmetric and to write them on binary tape.

C ← FOR COMMENT		CONTINUATION	FORTRAN STATEMENT				IDENTIFICATION	
STATEMENT NUMBER								
1	5	6	7			72	73	80
			REWIND 3					
			DO 3 I = 1,N					
			DO 3 J = 1,N					
			IF(A(I,J)-A(J,I)) 3,20,3					
	3		CONTINUE					
			END FILE 3					
			MORE PROGRAM					
	20		IF(I-J) 21,3,21					
	21		WRITE TAPE 3,I,J, A(I,J)					
			GO TO 3					

After rewinding tape 3, a nested pair of DO loops scans the entire matrix for elements  $A(I,J)$  equal to  $A(J,I)$ . Whenever such an element is found an exit completely out of the nest is made to a routine which for off-diagonal elements only writes a 3-word record (I, J, and  $A(I,J)$ ) in binary on tape 3. Both for on- and off-diagonal elements this routine makes no change in the indexes or indexing parameters of the nest, and so it is permissible to re-enter the nest and continue the scan.

This program actually finds each element twice. This could be avoided by writing the second DO as  $DO\ 3\ J = I,N$ .

## APPENDIX A. TABLE OF FORTRAN CHARACTERS

				CARD	BCD TAPE	704					CARD	BCD TAPE	704					CARD	BCD TAPE	704					CARD	BCD TAPE	704
1	1	01	01	A	$\begin{matrix} 12 \\ 1 \end{matrix}$	61	21	J	$\begin{matrix} 11 \\ 1 \end{matrix}$	41	41	/	$\begin{matrix} 0 \\ 1 \end{matrix}$	21	61												
2	2	02	02	B	$\begin{matrix} 12 \\ 2 \end{matrix}$	62	22	K	$\begin{matrix} 11 \\ 2 \end{matrix}$	42	42	S	$\begin{matrix} 0 \\ 2 \end{matrix}$	22	62												
3	3	03	03	C	$\begin{matrix} 12 \\ 3 \end{matrix}$	63	23	L	$\begin{matrix} 11 \\ 3 \end{matrix}$	43	43	T	$\begin{matrix} 0 \\ 3 \end{matrix}$	23	63												
4	4	04	04	D	$\begin{matrix} 12 \\ 4 \end{matrix}$	64	24	M	$\begin{matrix} 11 \\ 4 \end{matrix}$	44	44	U	$\begin{matrix} 0 \\ 4 \end{matrix}$	24	64												
5	5	05	05	E	$\begin{matrix} 12 \\ 5 \end{matrix}$	65	25	N	$\begin{matrix} 11 \\ 5 \end{matrix}$	45	45	V	$\begin{matrix} 0 \\ 5 \end{matrix}$	25	65												
6	6	06	06	F	$\begin{matrix} 12 \\ 6 \end{matrix}$	66	26	O	$\begin{matrix} 11 \\ 6 \end{matrix}$	46	46	W	$\begin{matrix} 0 \\ 6 \end{matrix}$	26	66												
7	7	07	07	G	$\begin{matrix} 12 \\ 7 \end{matrix}$	67	27	P	$\begin{matrix} 11 \\ 7 \end{matrix}$	47	47	X	$\begin{matrix} 0 \\ 7 \end{matrix}$	27	67												
8	8	10	10	H	$\begin{matrix} 12 \\ 8 \end{matrix}$	70	30	Q	$\begin{matrix} 11 \\ 8 \end{matrix}$	50	50	Y	$\begin{matrix} 0 \\ 8 \end{matrix}$	30	70												
9	9	11	11	I	$\begin{matrix} 12 \\ 9 \end{matrix}$	71	31	R	$\begin{matrix} 11 \\ 9 \end{matrix}$	51	51	Z	$\begin{matrix} 0 \\ 9 \end{matrix}$	31	71												
Blank		20	60	+	12	60	20	-	11	40	40	0	0	12	00												
=	8-3	13	13	.	$\begin{matrix} 12 \\ 8-3 \end{matrix}$	73	33	\$	$\begin{matrix} 11 \\ 8-3 \end{matrix}$	53	53	,	$\begin{matrix} 0 \\ 8-3 \end{matrix}$	33	73												
-	8-4	14	14	)	$\begin{matrix} 12 \\ 8-4 \end{matrix}$	74	34	*	$\begin{matrix} 11 \\ 8-4 \end{matrix}$	54	54	(	$\begin{matrix} 0 \\ 8-4 \end{matrix}$	34	74												

NOTE 1. There are two - signs. Only the 11-punch may be used in source program cards. Either minus may be used in input data to the object program; object program output has the 11 minus.

NOTE 2. The \$ character can be used in FORTRAN only as Hollerith text in a FORMAT statement.

## APPENDIX B. TABLE OF FORTRAN STATEMENTS

STATEMENT	NORMAL SEQUENCING
$a = b$	Next executable statement
GO TO n	Statement n
GO TO n, (n <sub>1</sub> ,n <sub>2</sub> ,...,n <sub>m</sub> )	Statement last assigned
ASSIGN i TO n	Next executable statement
GO TO (n <sub>1</sub> ,n <sub>2</sub> ,...,n <sub>m</sub> ), i	Statement n <sub>i</sub>
IF (a) n <sub>1</sub> ,n <sub>2</sub> ,n <sub>3</sub>	Statement n <sub>1</sub> ,n <sub>2</sub> ,n <sub>3</sub> as a less than, =, or greater than 0
SENSE LIGHT i	Next executable statement
IF (SENSE LIGHT i) n <sub>1</sub> ,n <sub>2</sub>	Statement n <sub>1</sub> ,n <sub>2</sub> as Sense Light i ON or OFF
IF (SENSE SWITCH i) n <sub>1</sub> ,n <sub>2</sub>	“ “ “ as Sense Switch i DOWN or UP
IF ACCUMULATOR OVERFLOW n <sub>1</sub> ,n <sub>2</sub>	“ “ “ as Accumulator Overflow trigger ON or OFF
IF QUOTIENT OVERFLOW n <sub>1</sub> ,n <sub>2</sub>	“ “ “ as MQ Overflow trigger ON or OFF
IF DIVIDE CHECK n <sub>1</sub> ,n <sub>2</sub>	“ “ “ as Divide Check trigger ON or OFF
PAUSE or PAUSE n	Next executable statement
STOP or STOP n	Terminates program
DO n i = m <sub>1</sub> ,m <sub>2</sub> or DO n i = m <sub>1</sub> ,m <sub>2</sub> ,m <sub>3</sub>	Next executable statement
CONTINUE	“ “ “
FORMAT (Specification)	Not executed
READ n, List	Next executable statement
READ INPUT TAPE i, n, List	“ “ “
PUNCH n, List	“ “ “
PRINT n, List	“ “ “
WRITE OUTPUT TAPE i, n, List	“ “ “
READ TAPE i, List	“ “ “
READ DRUM i, j, List	“ “ “
WRITE TAPE i, List	“ “ “
WRITE DRUM i, j, List	“ “ “
END FILE i	“ “ “
REWIND i	“ “ “
BACKSPACE i	“ “ “
DIMENSION v, v, v, . . . .	Not executed
EQUIVALENCE (a,b,c, . . .), (d,e,f, . . .), . . .	“ “
FREQUENCY n(i,j, . . .), m(k,l, . . .), . . .	“ “

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